



# Bayesian Language Games

Unifying and evaluating agent-based models  
of horizontal and vertical language evolution

**Bas Cornelissen**



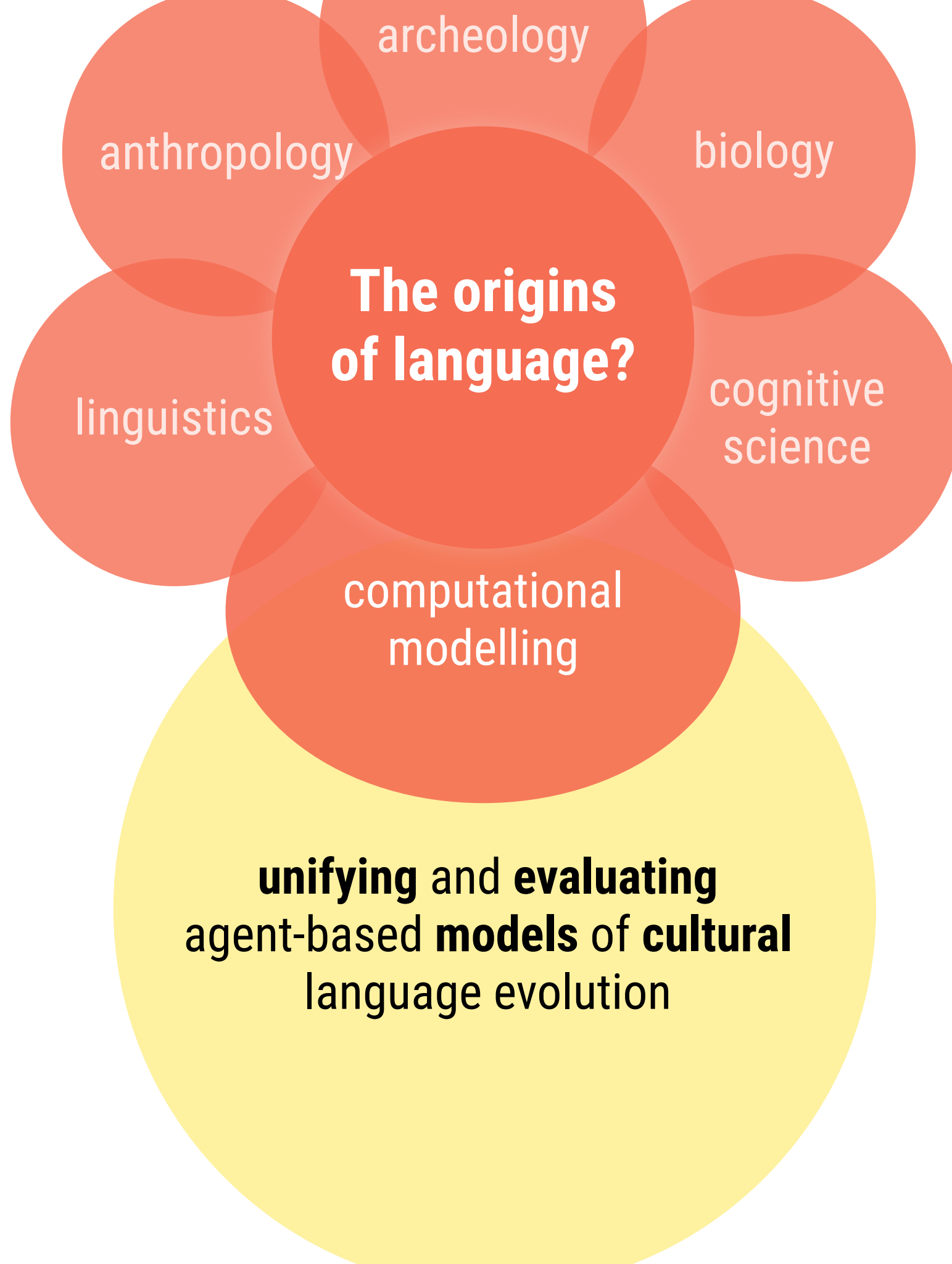


**The (Little) Tower of Babel** by **Pieter Bruegel the Elder** (c. 1563) oil on panel; 60 cm × 74.5 cm; Museum Boijmans Van Beuningen, Rotterdam



## THE CENTRAL PROBLEM

**Sound does not fossilise.**



**NO LANGUAGE**

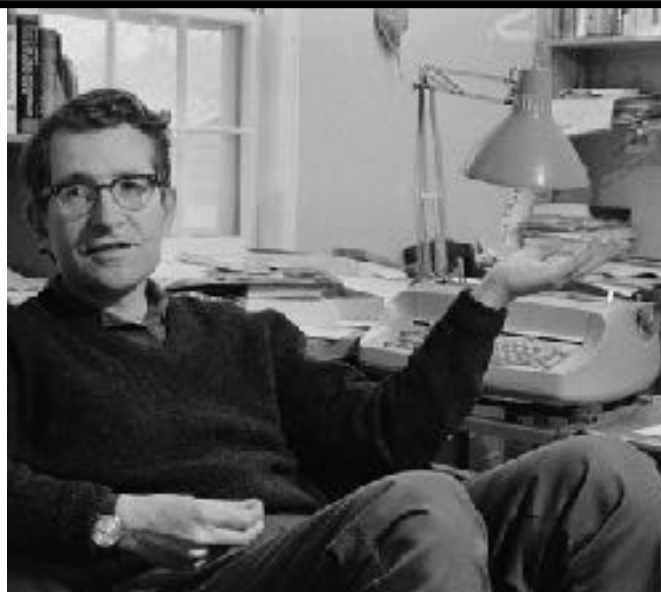
**LANGUAGE**

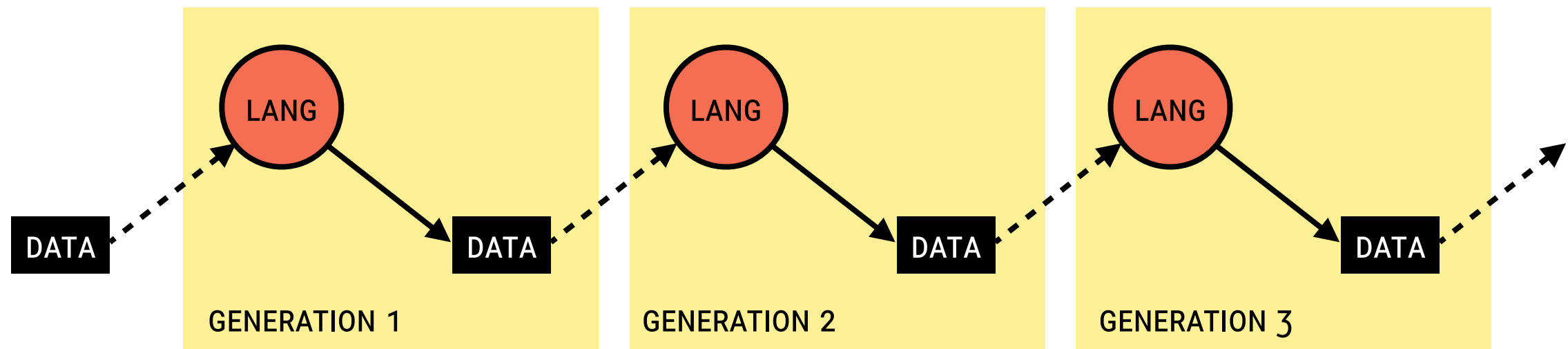
cultural  
evolution

cultural  
evolution

biological  
evolution

time

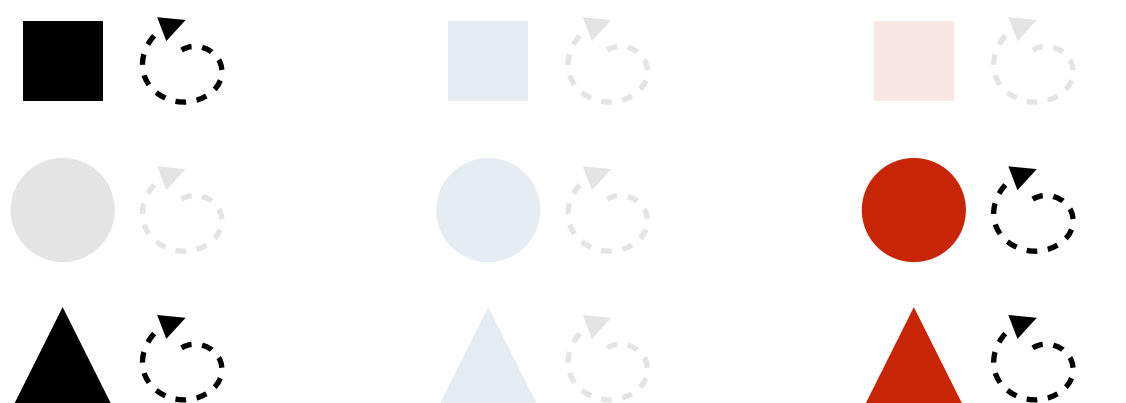
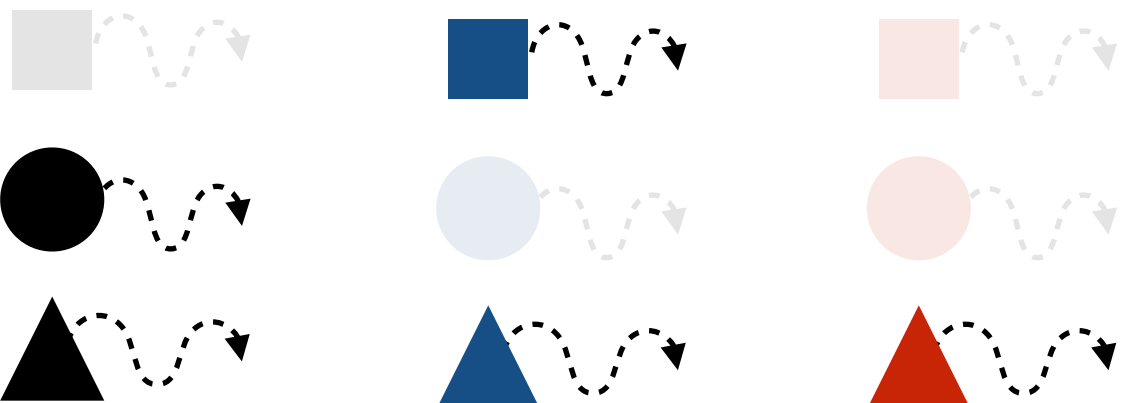
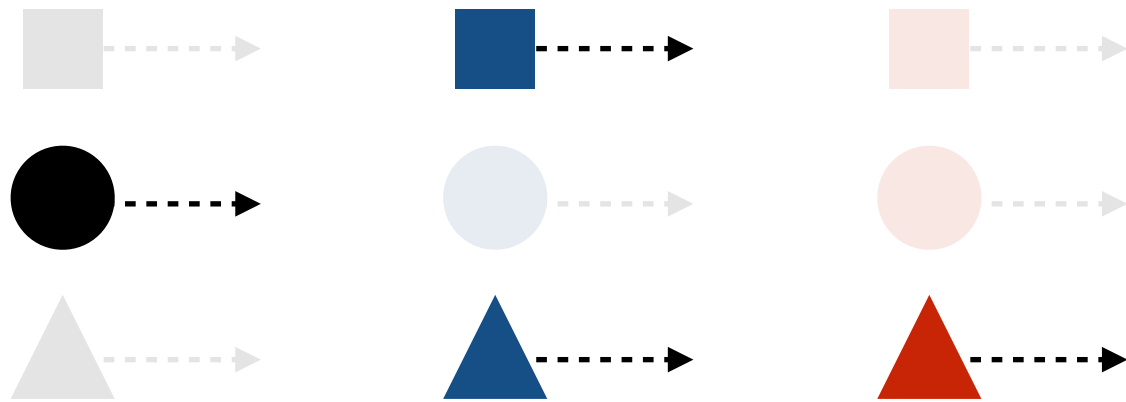




## Iterated learning

Every generation learns the language spoken by the previous generation.

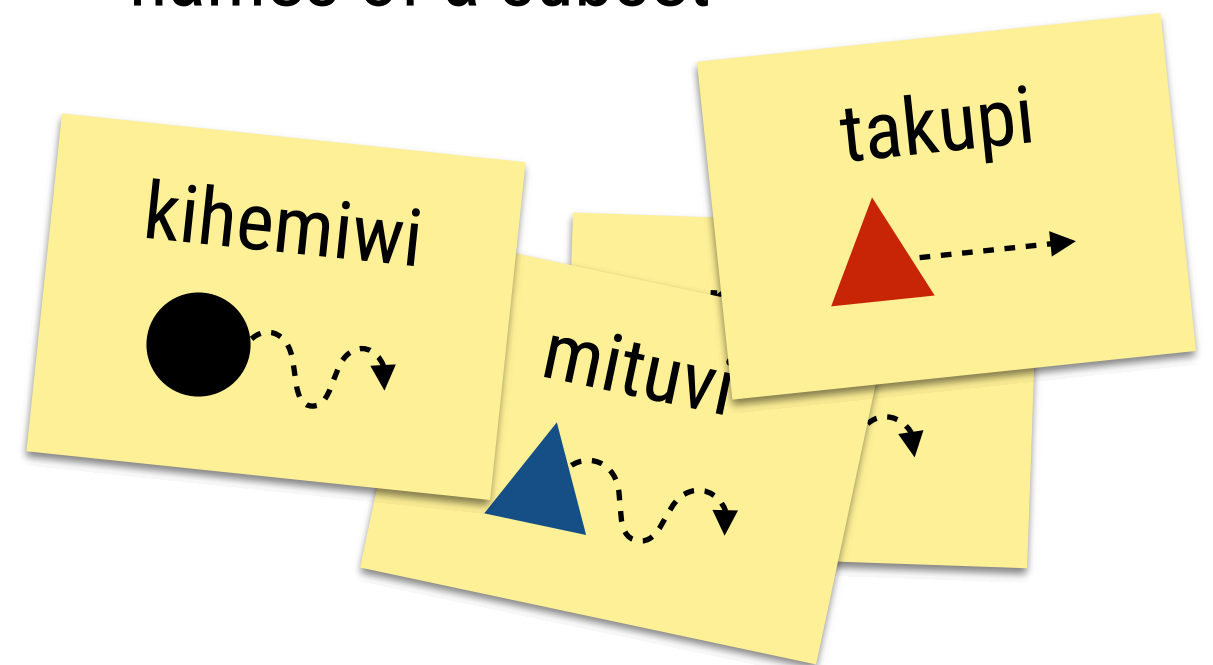
**Vertical** transmission across generations



## Emerging compositionality

Use the objects in different contexts, including errors, to train with the next subject

1. **Train** subject to learn the names of a subset



2. **Test** the subject on the full set of objects

→	n-ere-ki	l-ere-ki	renana
	n-ehe-ki	l-aho-ki	r-ene-ki
	n-eke-ki	l-ake-ki	r-ahe-ki
↗	n-ere-plo	l-ane-plo	r-e-plo
	n-eho-plo	l-aho-plo	r-eho-plo
	n-eki-plo	l-aki-plo	r-aho-plo
↻	n-e-pilu	l-ane-pilu	r-e-pilu
	n-eho-pilu	l-aho-pilu	r-eho-pilu
	n-eki-pilu	l-aki-pilu	r-aho-pilu

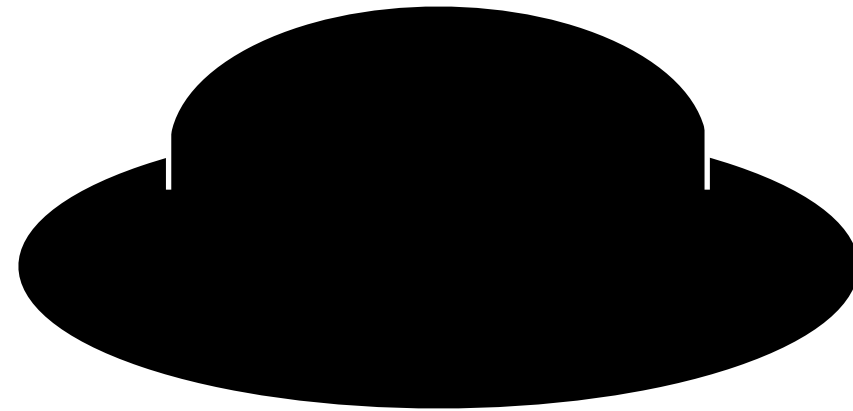
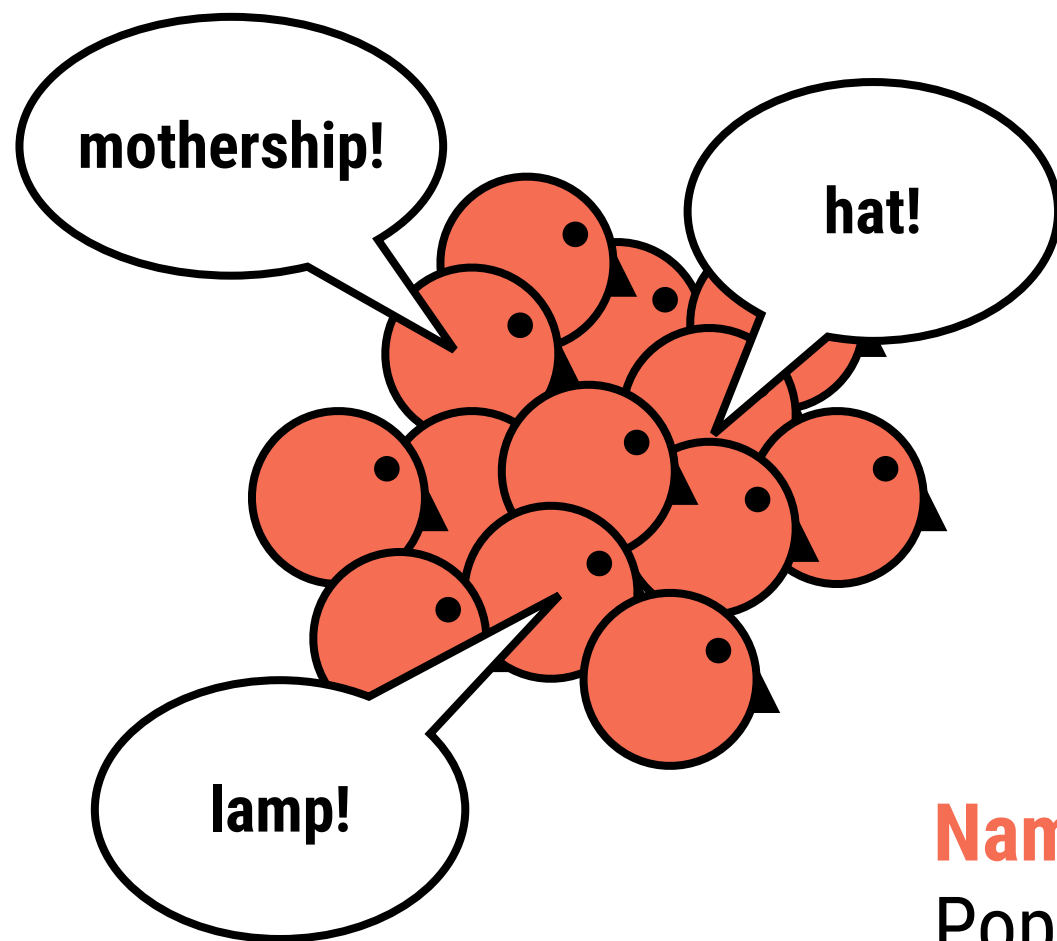


## Compositional language

Meaning of a signal determined by meaning of parts

Cultural processes (transmission & communication) pressure for compositional languages

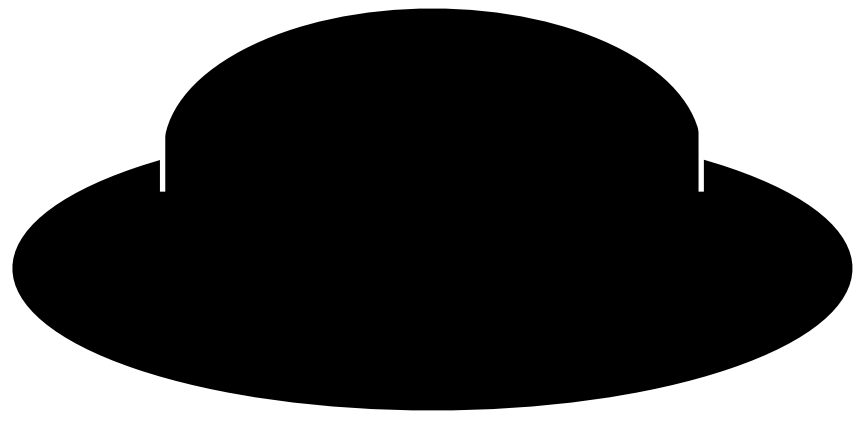
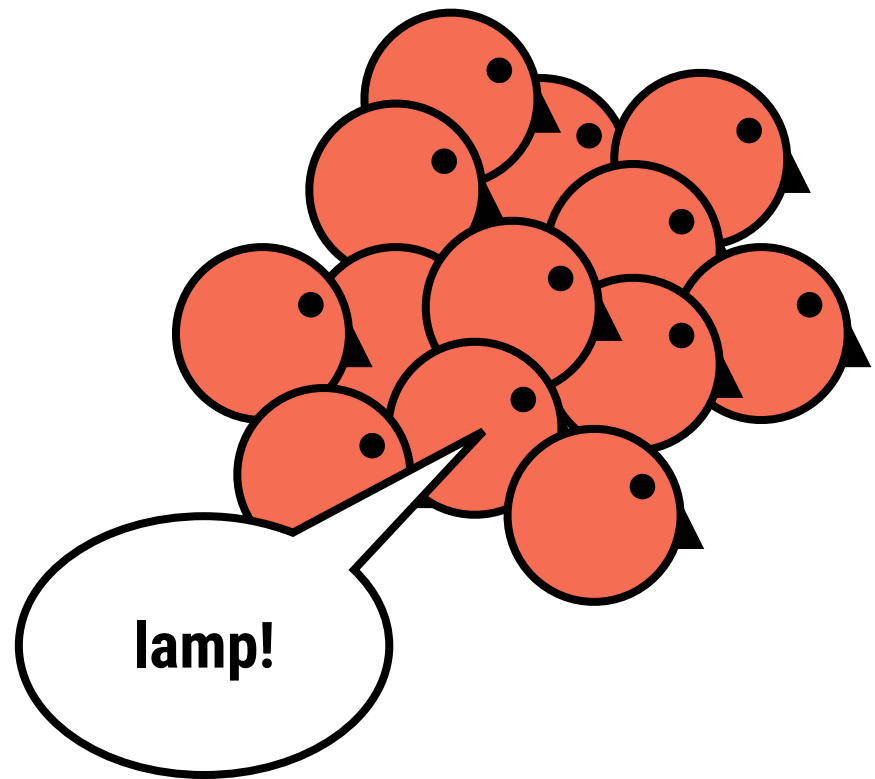




### **Naming game**

Population negotiates a shared convention via local interactions:

1. Select random speaker & hearer
2. The hearer utters a word.
3. Both agents 'align' languages



**Minimal NG**

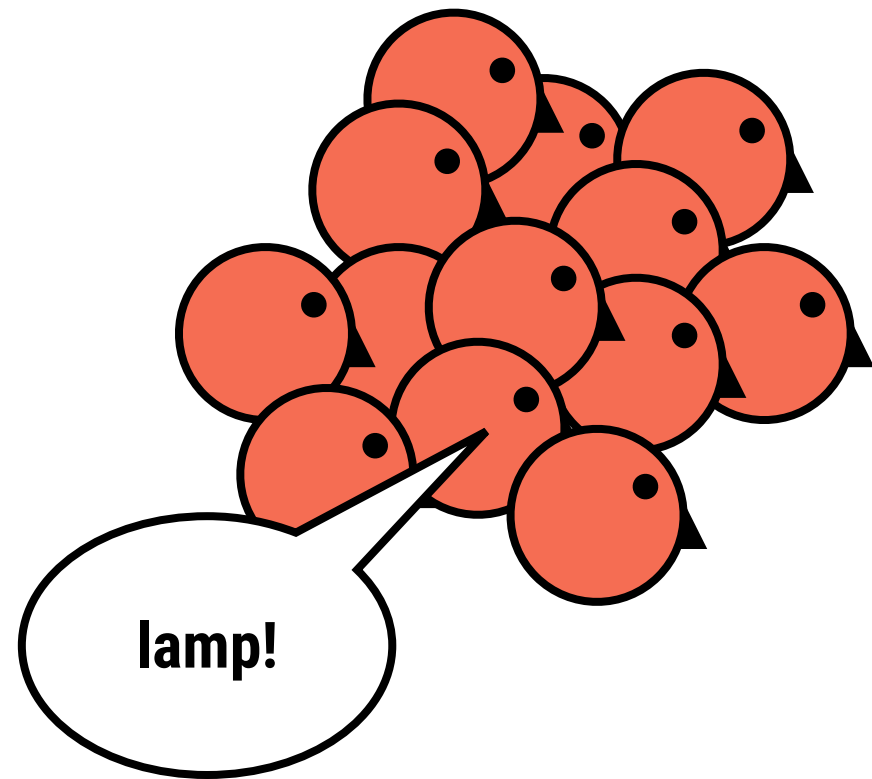
Every agent can **invent, add** and **remove** words to its vocabulary

**Success**

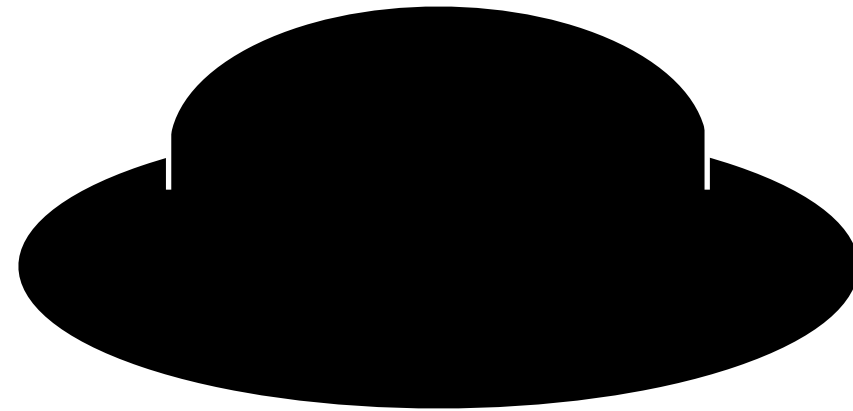
SPEAKER	HEARER		SPEAKER	HEARER
hat	<b>lamp</b>	→	<b>lamp</b>	<b>lamp</b>
ship	hat			
<b>lamp</b>				

**Failure**

SPEAKER	HEARER		SPEAKER	HEARER
hat	hat	→	hat	hat
ship			ship	<b>lamp</b>
<b>lamp</b>			<b>lamp</b>	



**Success**



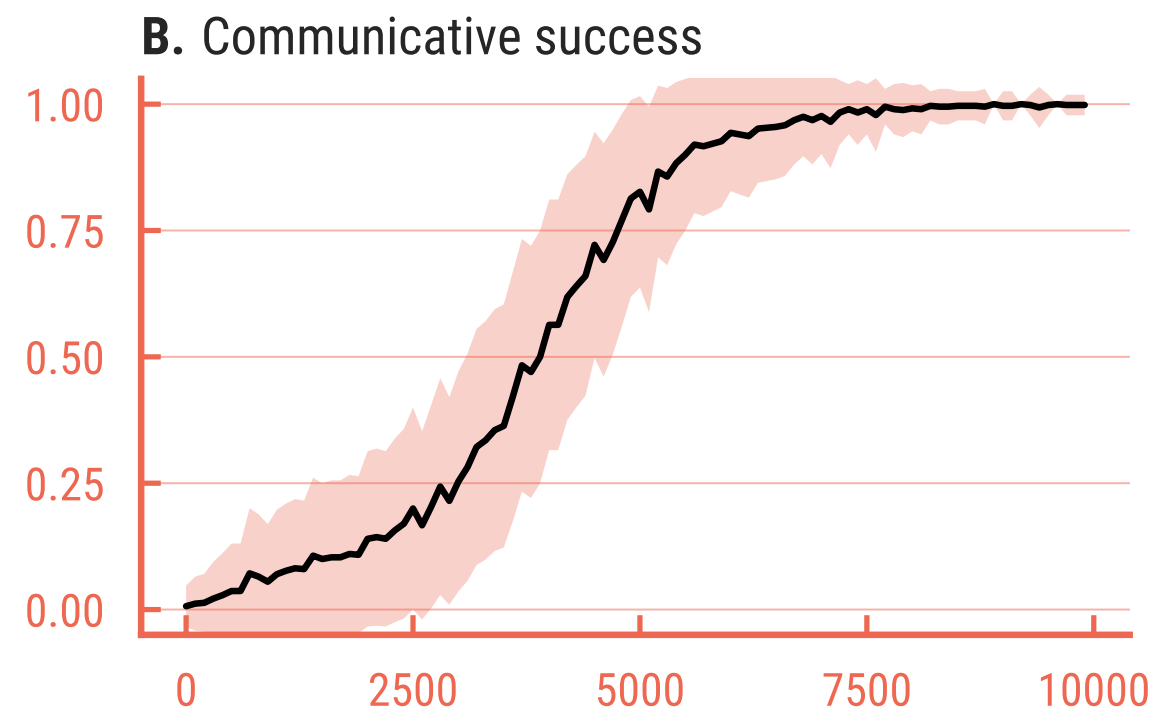
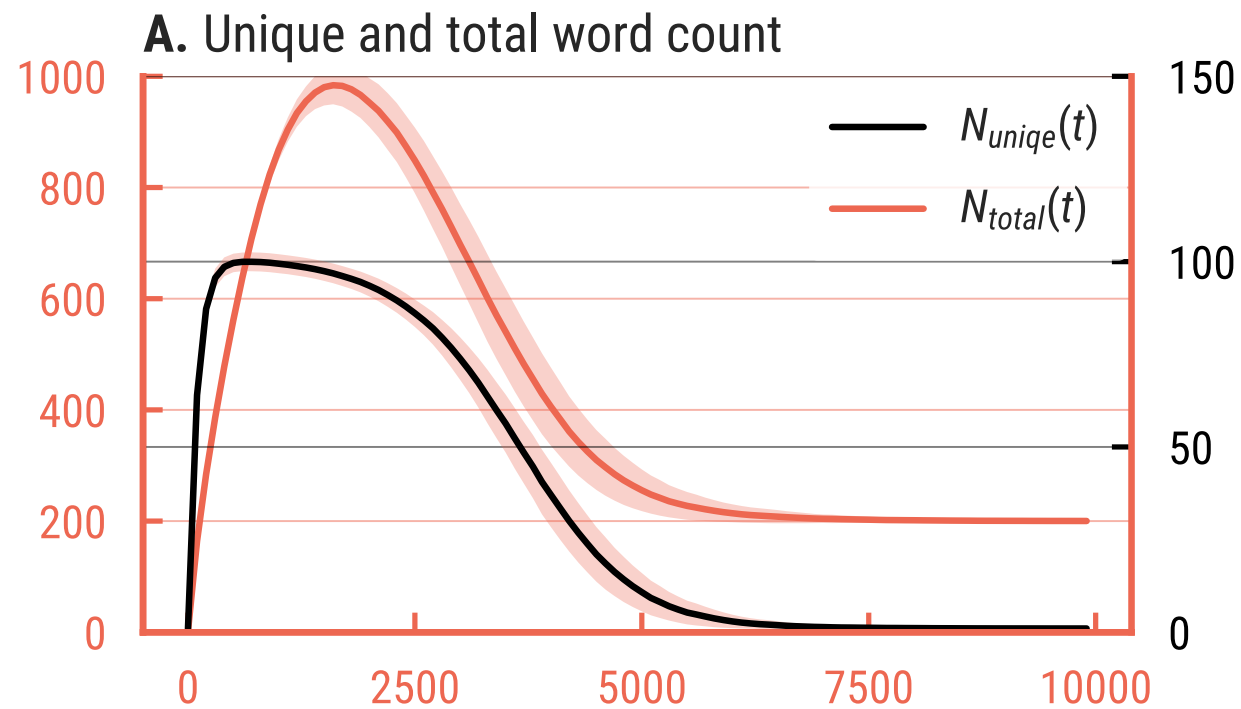
SPEAKER	HEARER
hat 0.4	<b>lamp 0.1</b>
ship 0.3	hat 0.2
<b>lamp 0.2</b>	



SPEAKER	HEARER
hat 0.3	<b>lamp 0.3</b>
ship 0.2	hat 0.1
<b>lamp 0.4</b>	

### **Lateral inhibition**

After success, decrease the scores of competing words

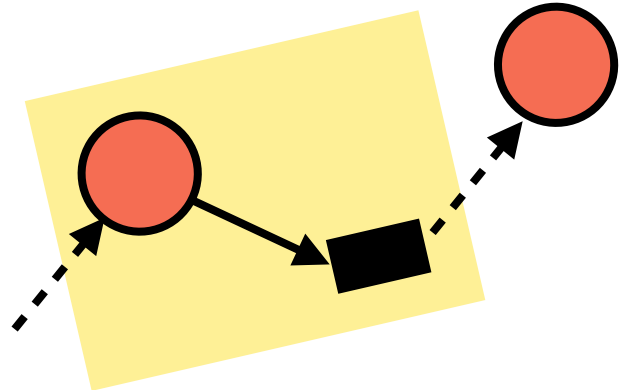
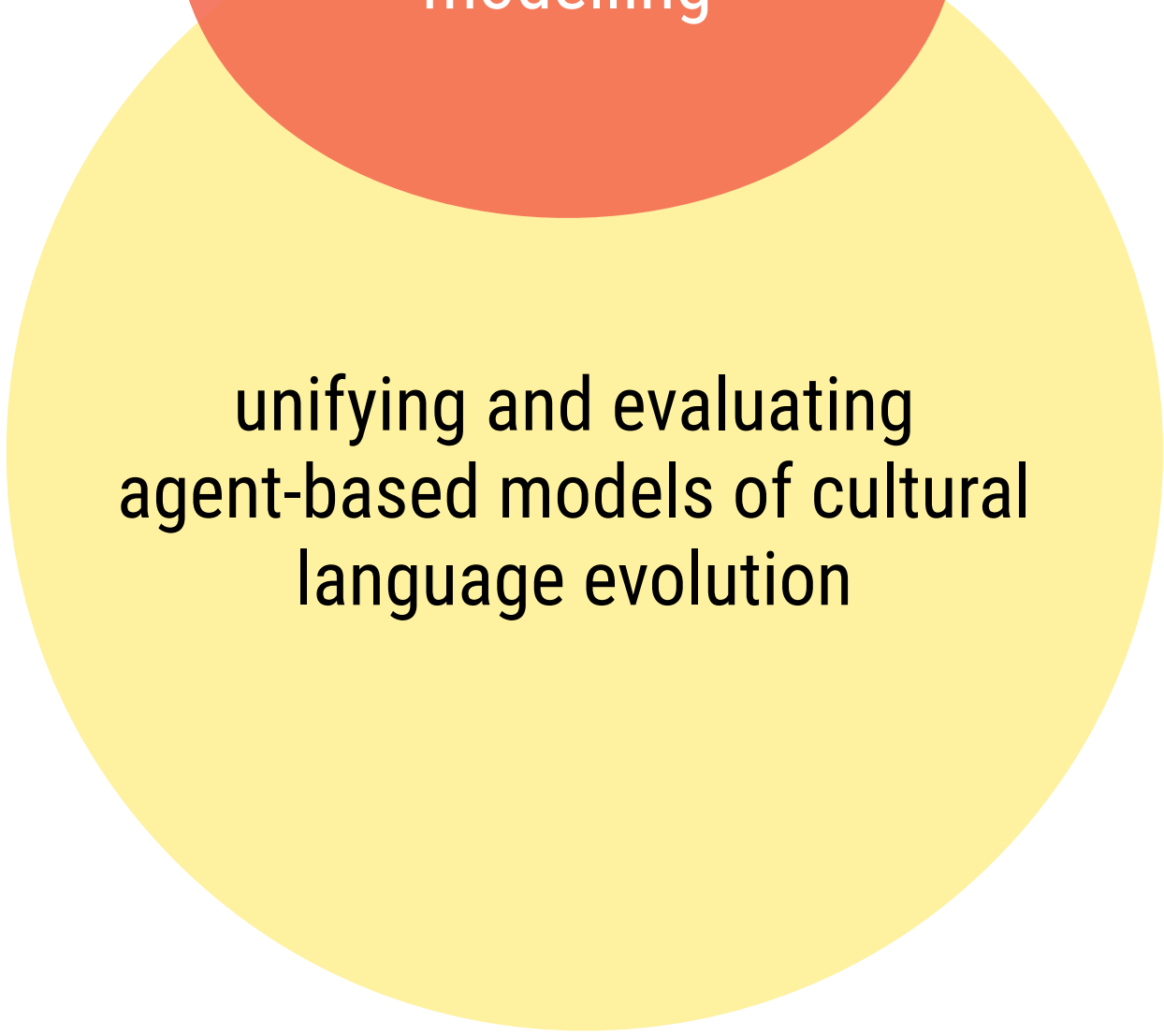
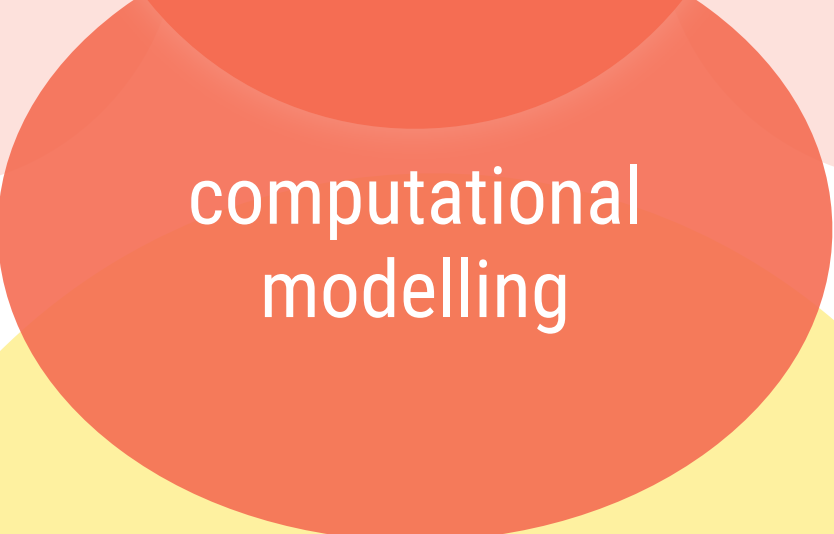


## Dynamics of the minimal NG

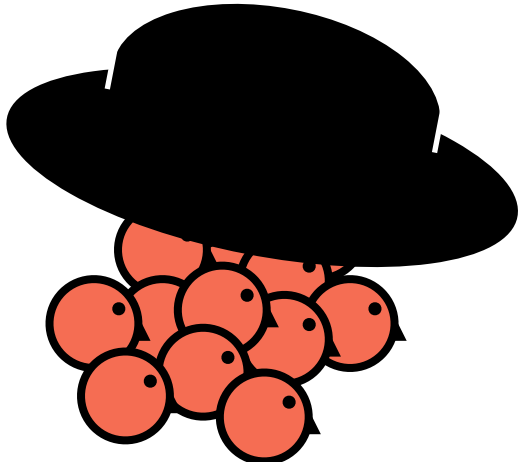
Three stages lead to the convergence to a single word:

1. Invention of words
2. Spread through population
3. Elimination of words

Cultural process of social negotiation leads to shared emergence of a convention

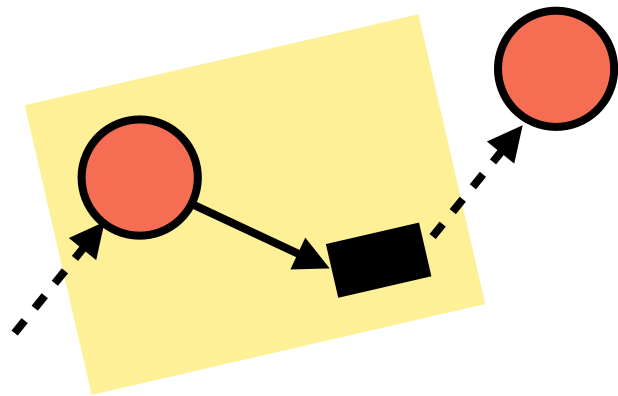


VERTICAL iterated learning

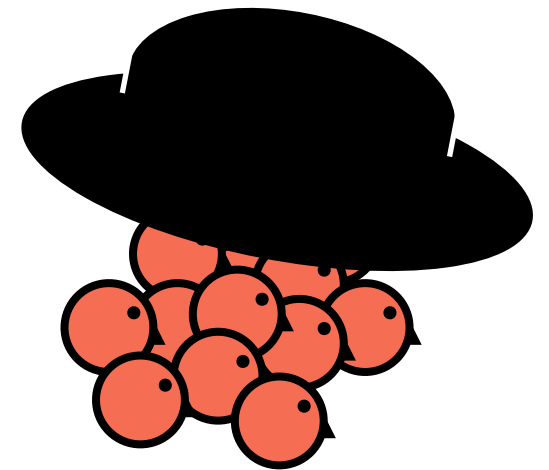
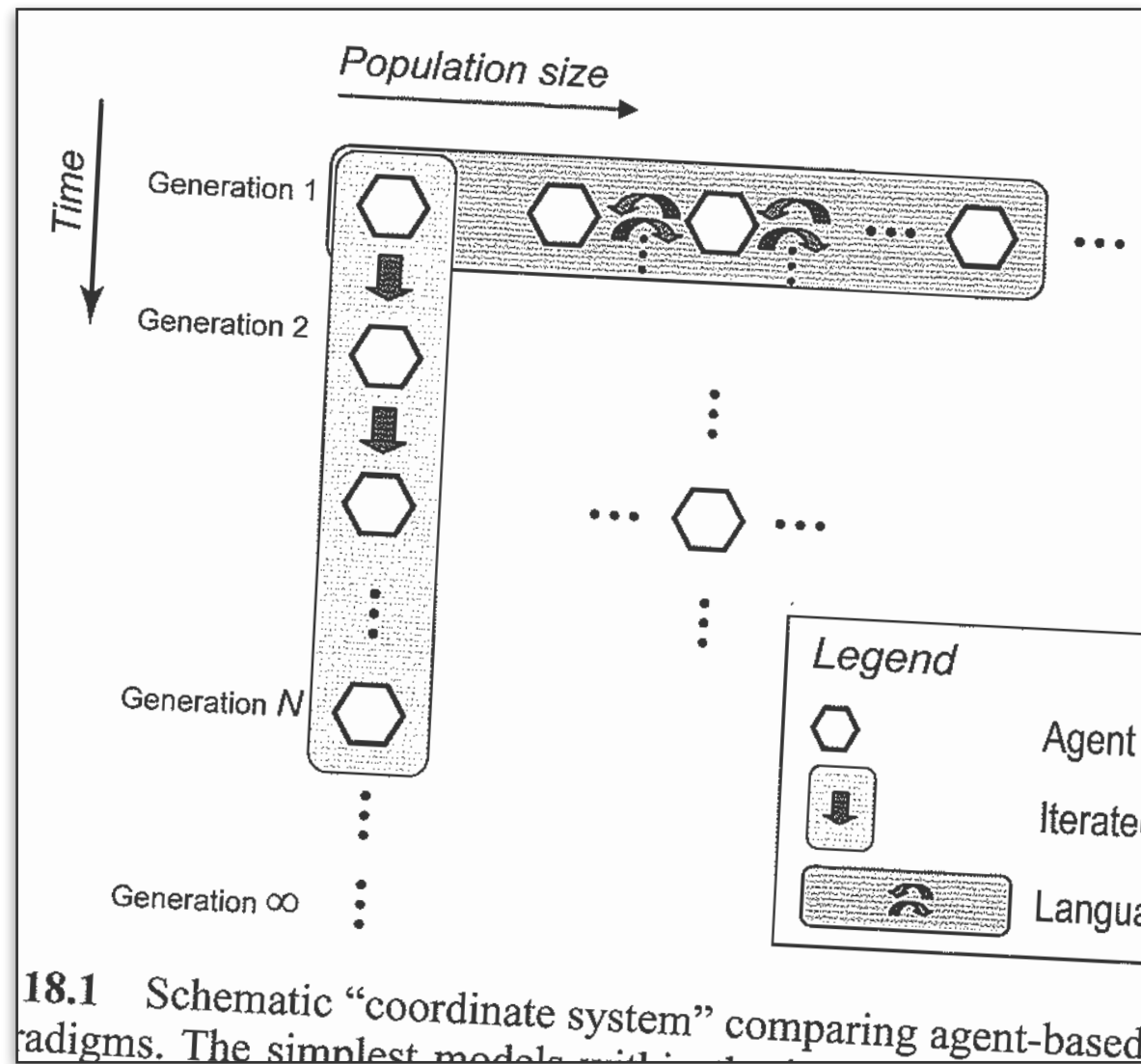


HORIZONTAL naming game

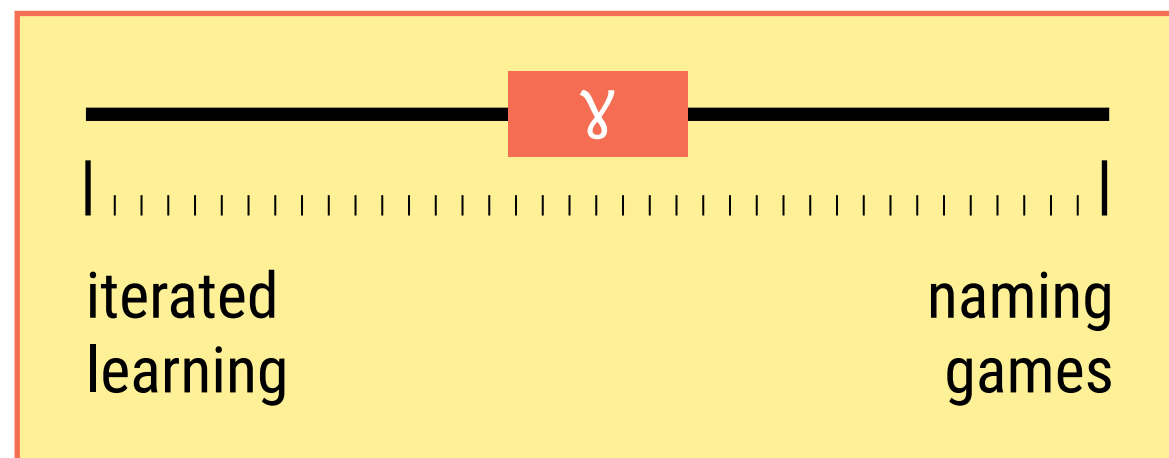




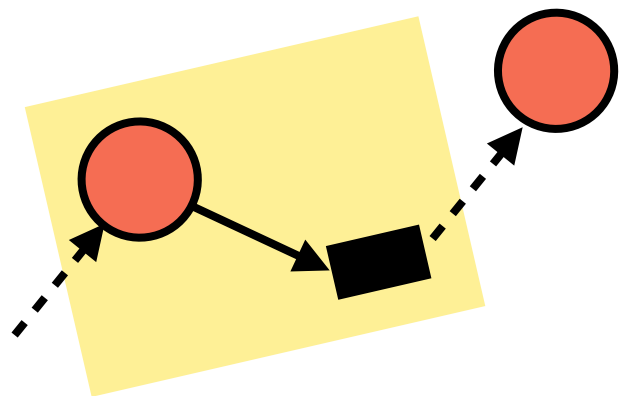
VERTICAL  
iterated learning



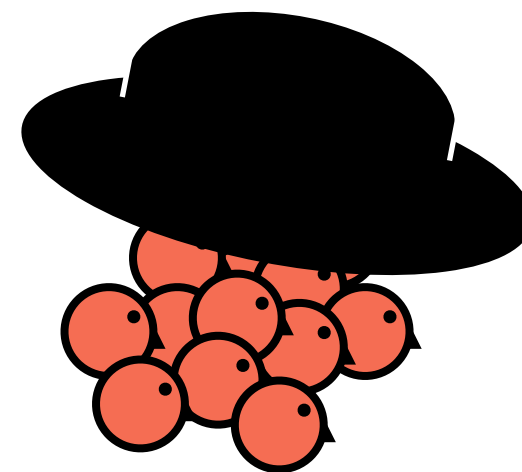
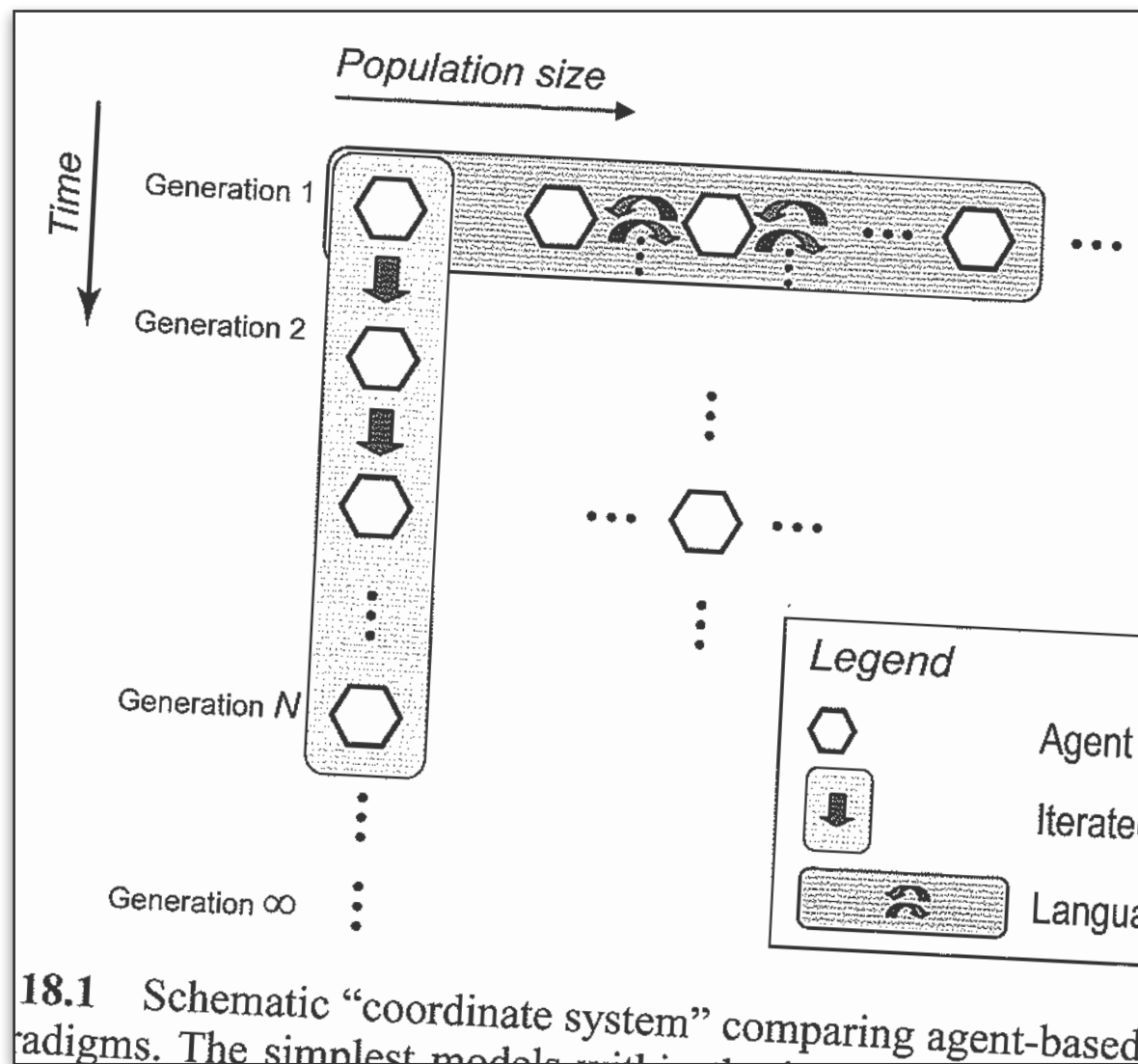
HORIZONTAL  
naming game



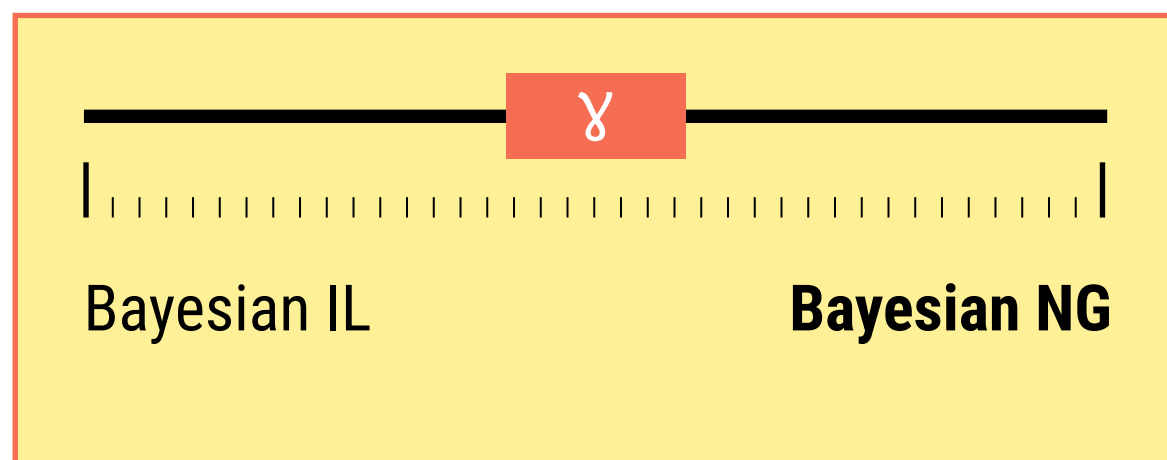
1. shared formalism    2. population model



VERTICAL  
iterated learning



HORIZONTAL  
naming game

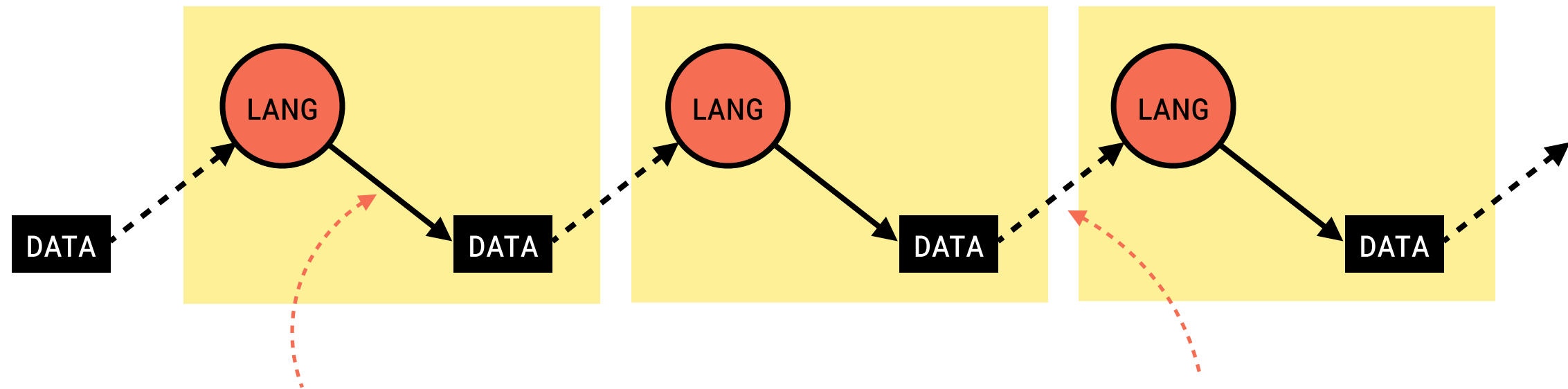


BAYESIAN  
LANGUAGE  
GAME

1. shared formalism
2. population model

# 1. Shared (Bayesian) formalism

# 2. Population model



production algorithm  
 $p(\text{data} \mid \text{lang})$

learning algorithm  
 $p(\text{lang} \mid \text{data})$

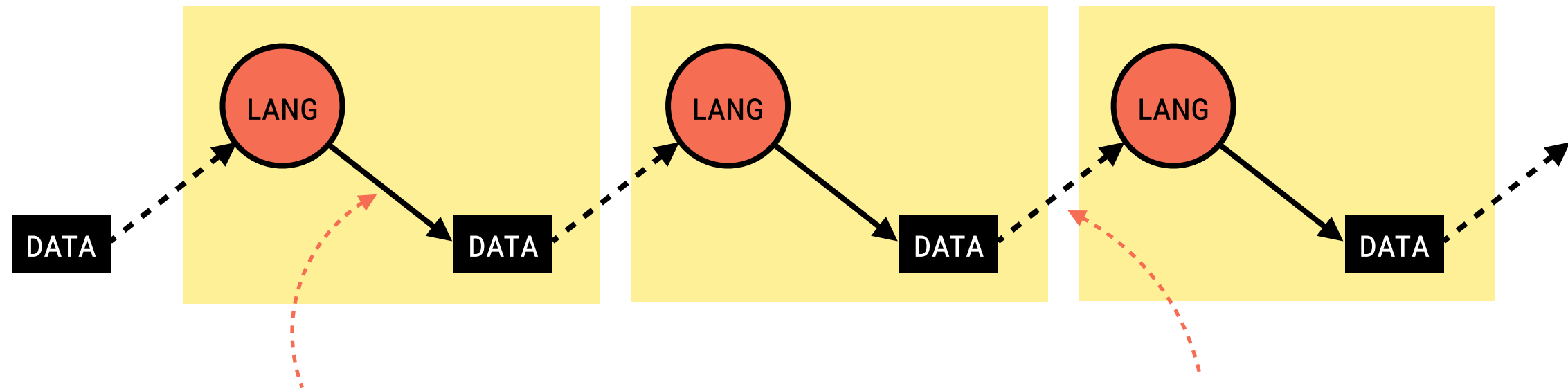
$$p(\text{lang} \mid \text{data}) \propto p(\text{data} \mid \text{lang}) \cdot p(\text{lang})$$

probability of  
adopting a language

biases of  
the learners

# 1. Shared (Bayesian) formalism

# 2. Population model



production algorithm  
 $p(\text{data} \mid \text{lang})$

learning algorithm  
 $p(\text{lang} \mid \text{data})$

$$p(\text{lang} \mid \text{data}) \propto p(\text{data} \mid \text{lang}) \cdot p(\text{lang})$$

probability of language  
after previous interaction

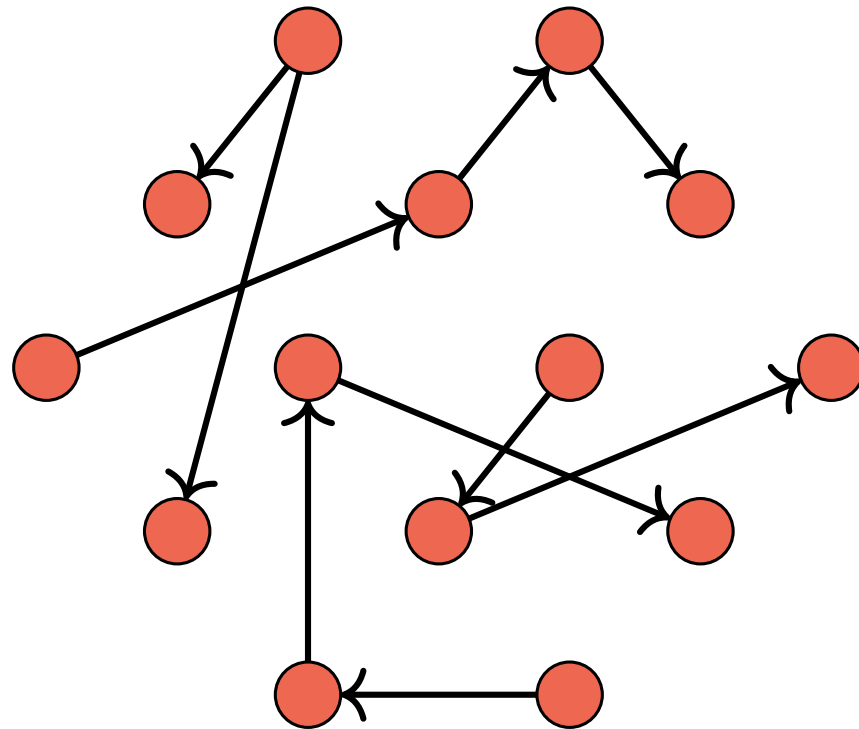
# 1. Shared (Bayesian) formalism

# 2. Population model

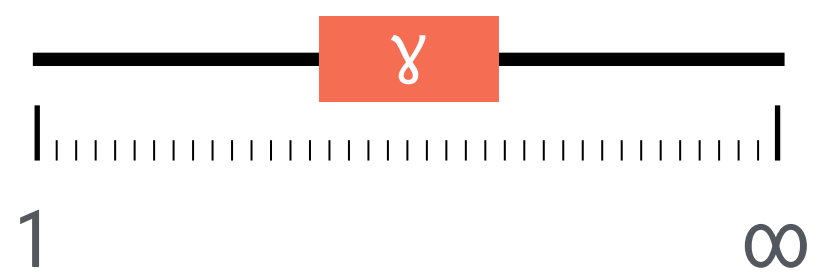
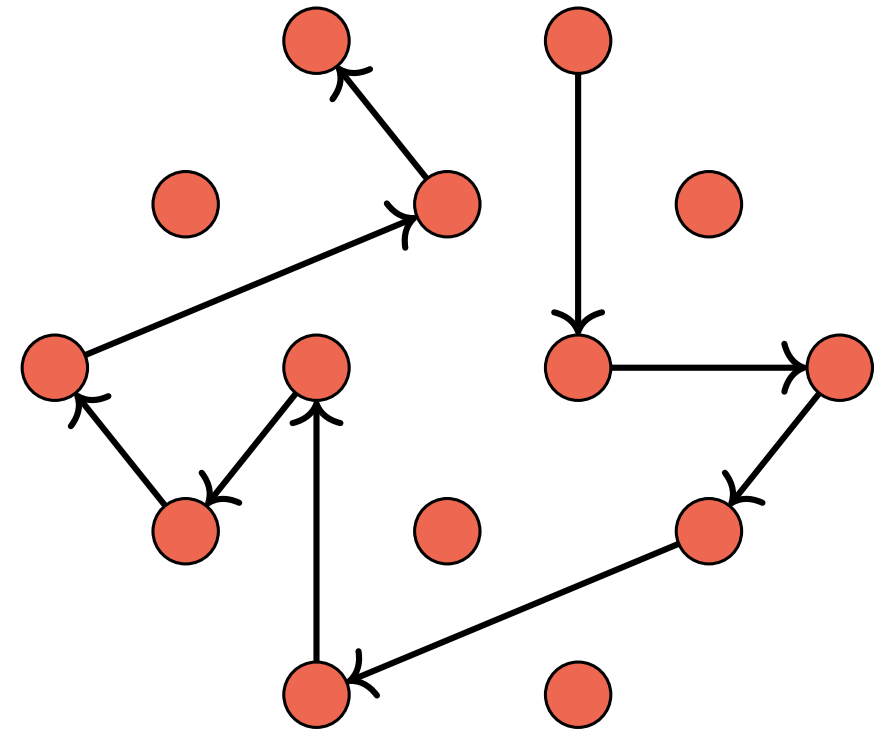
**VERTICAL**  
transmission chain



**HORIZONTAL**  
homogeneous mixing



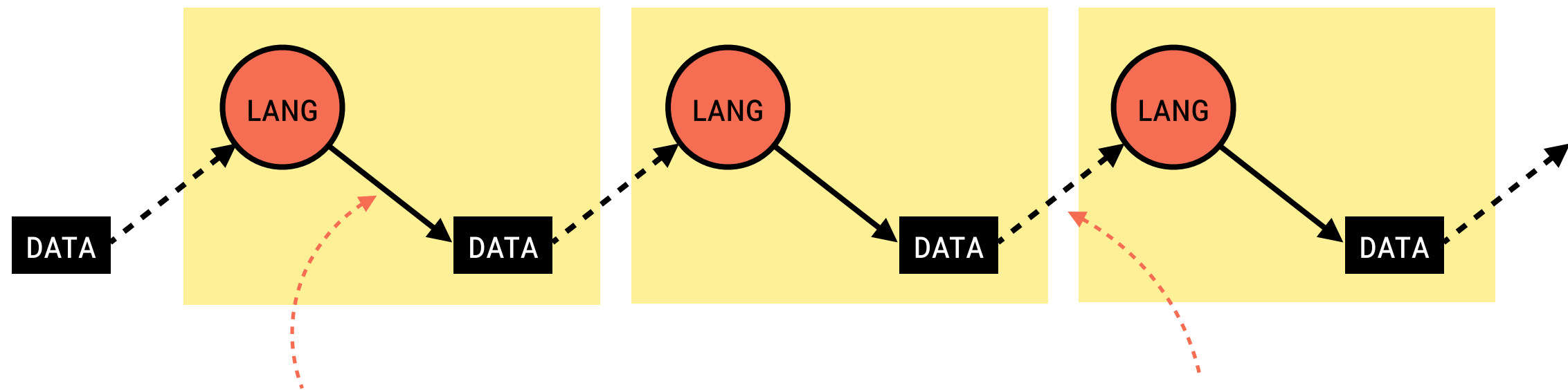
**BOTH**  
random walk



**LIFE EXPECTANCY  $\gamma$**   
The age at which a speaker dies

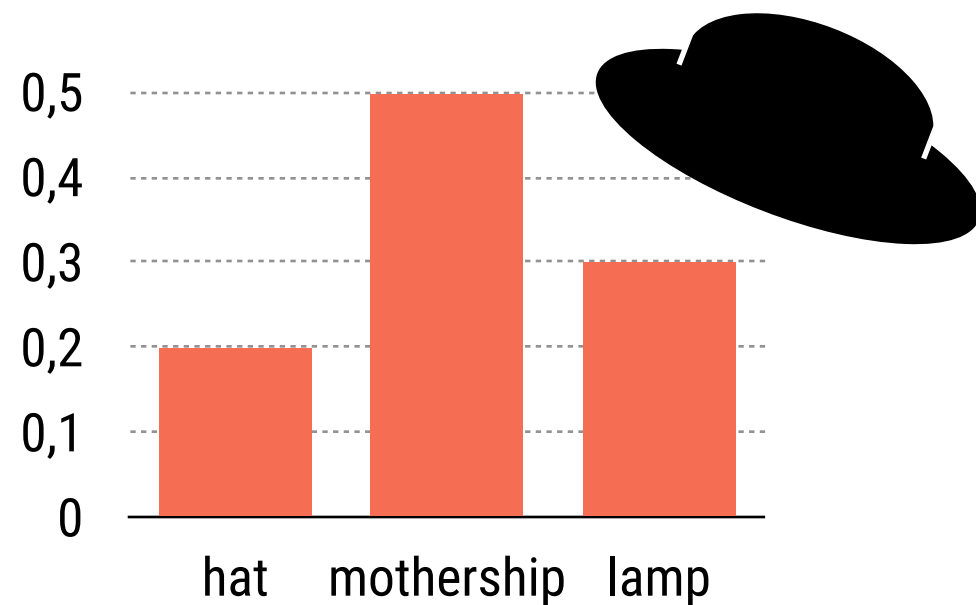


# The Bayesian Naming Game



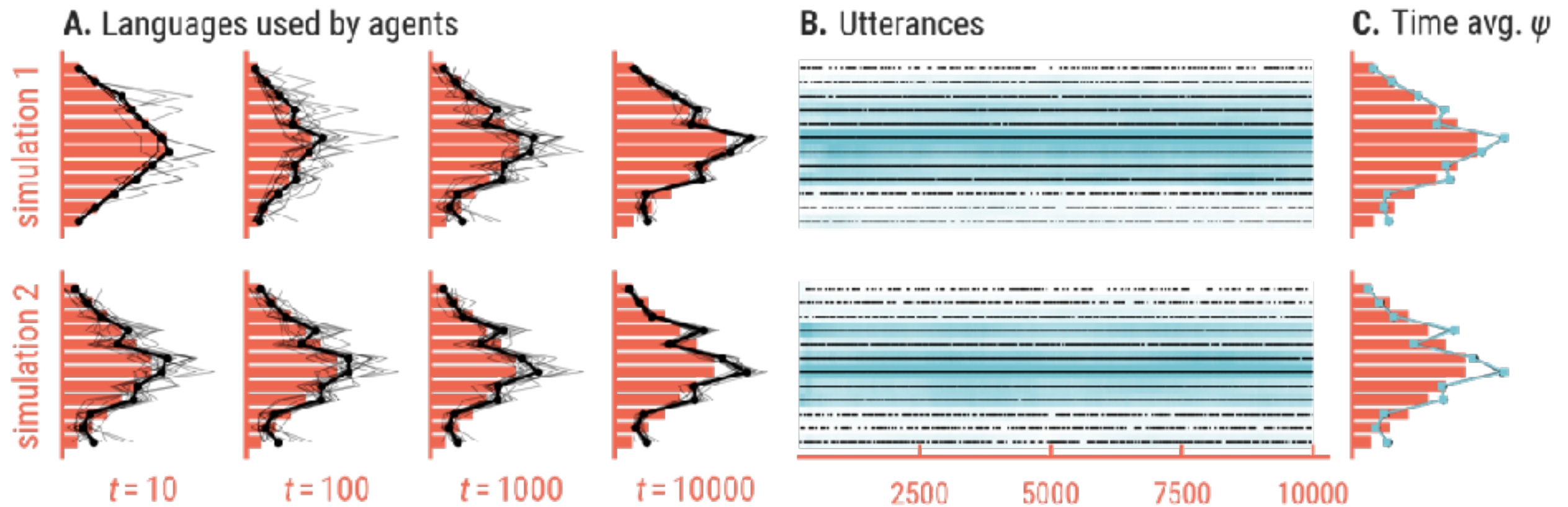
production algorithm  
 $p(\text{data} \mid \text{lang})$

learning algorithm  
 $p(\text{lang} \mid \text{data})$



A language is a  
distribution over words  
(or e.g. linguistic features)

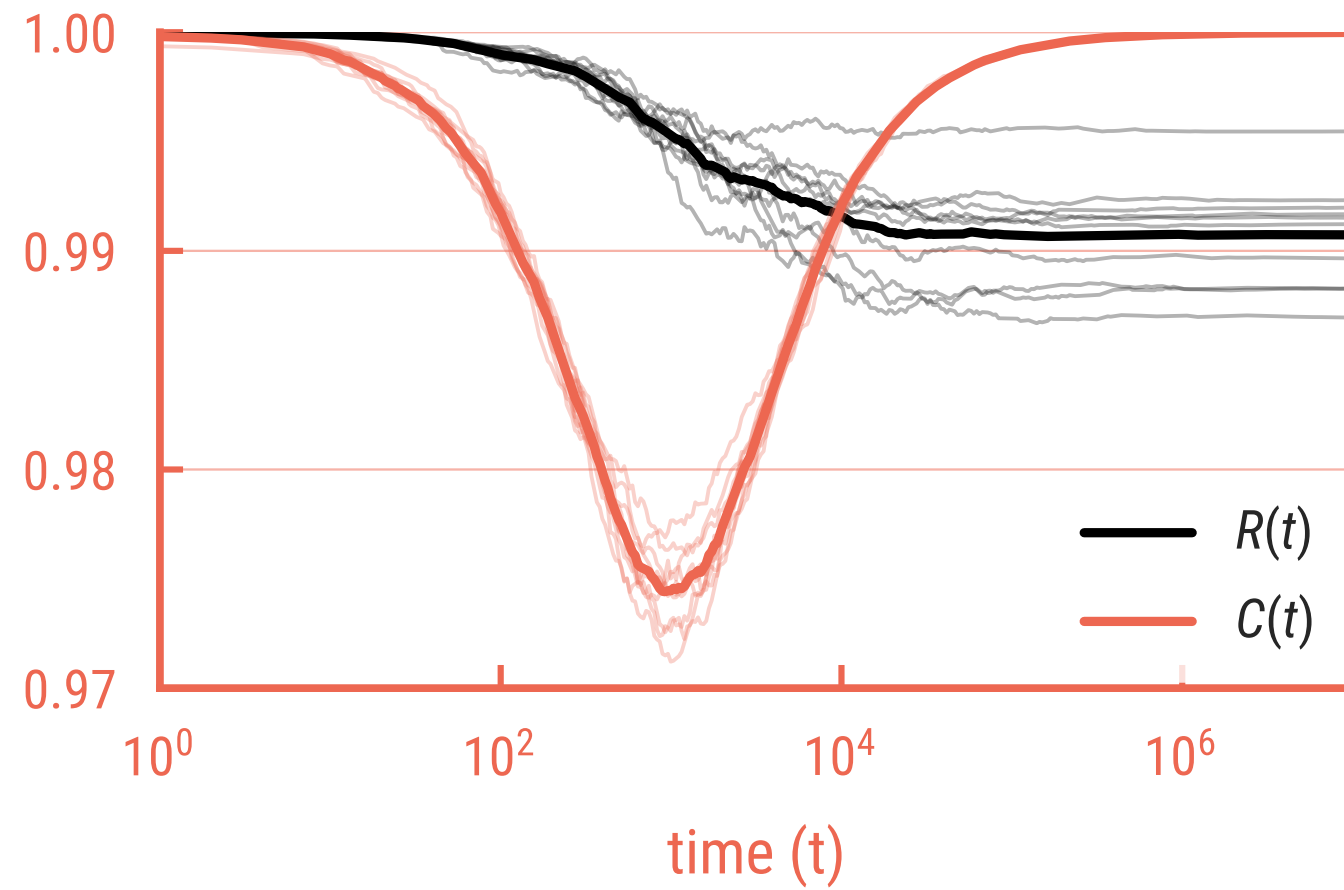
# The Bayesian Naming Game



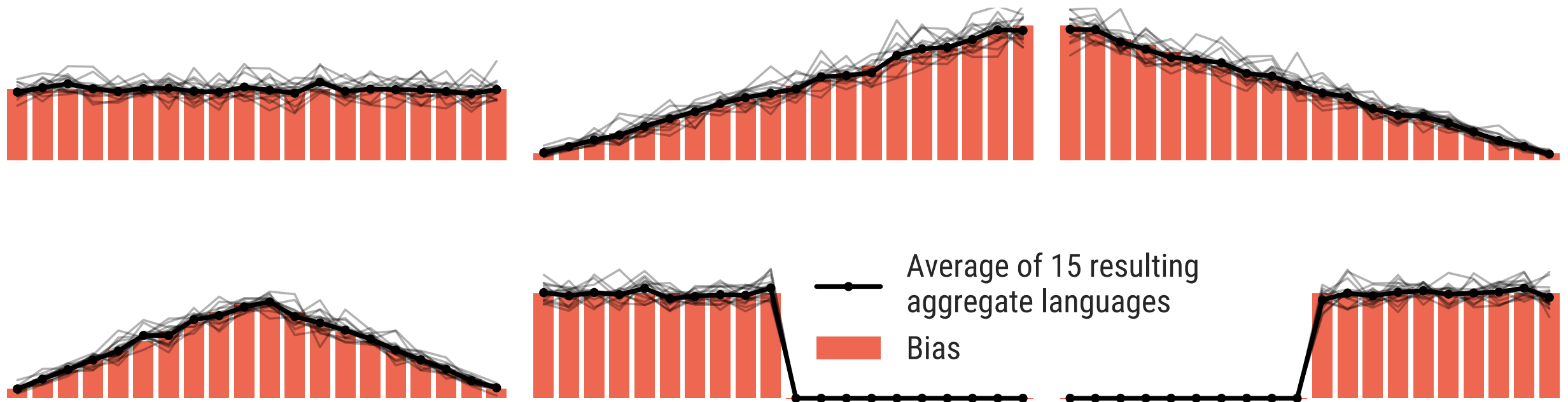
- Lineage specificity
- Reflection of the bias  
(rather than convergence to the prior)
- Language stability

# The Bayesian Naming Game

## B. Coherence and reflectance



# The Bayesian Naming Game



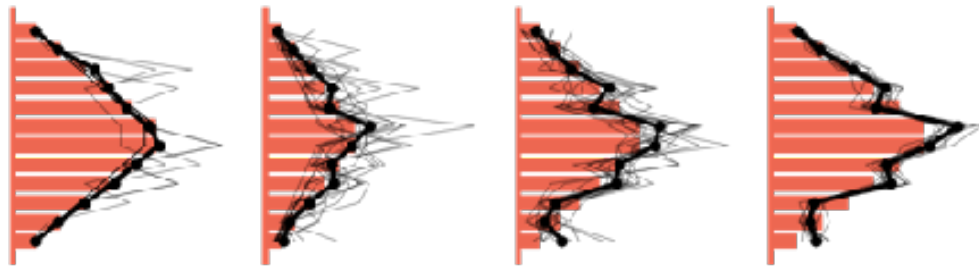
On average, the Bayesian Naming Game reproduces the innate biases.

Reminiscent of “wide but constrained variation” (e.g. colour terms)

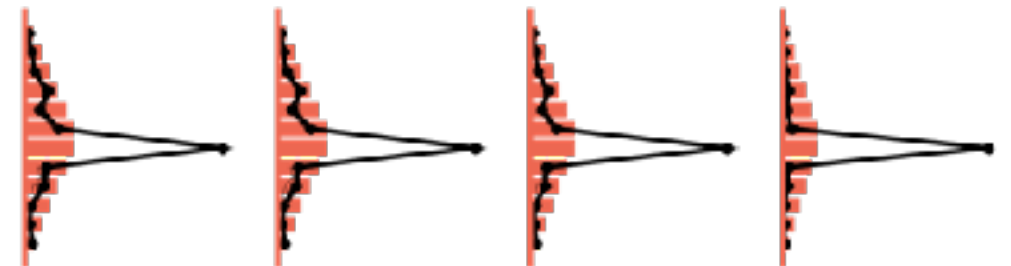
Regier et al. (2015). DOI [10.1002/9781118346136.ch11](https://doi.org/10.1002/9781118346136.ch11)

# Different strategies

But why this?

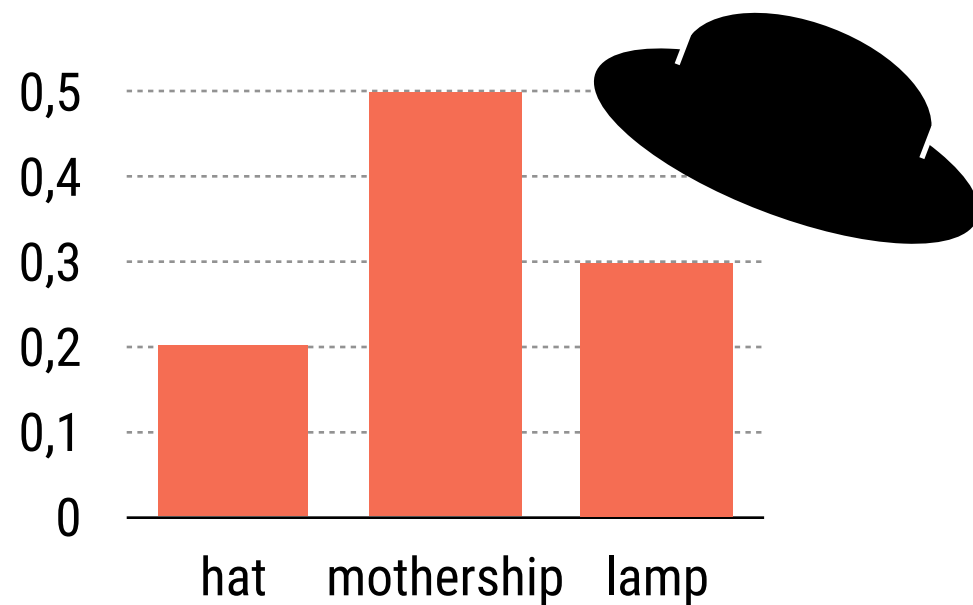


Shouldn't we expect this?



production algorithm

$$p(\text{data} \mid \text{lang})$$

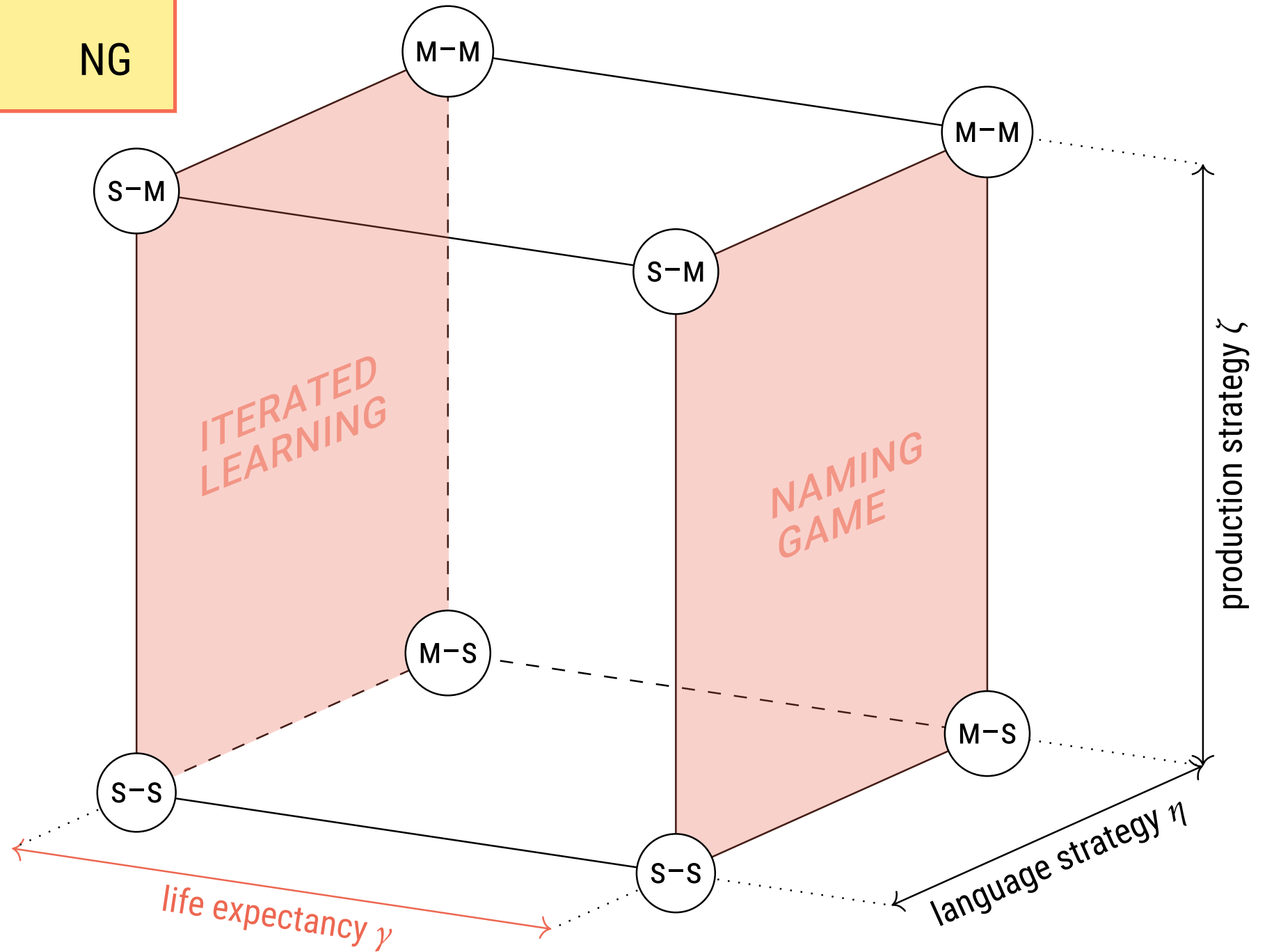
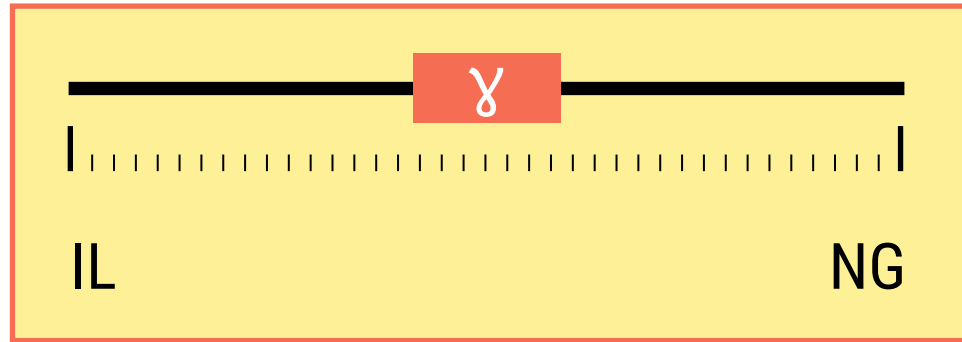


## Strategies

One can vary the 'production strategy' and 'language strategy'  
**sample** or **maximise**

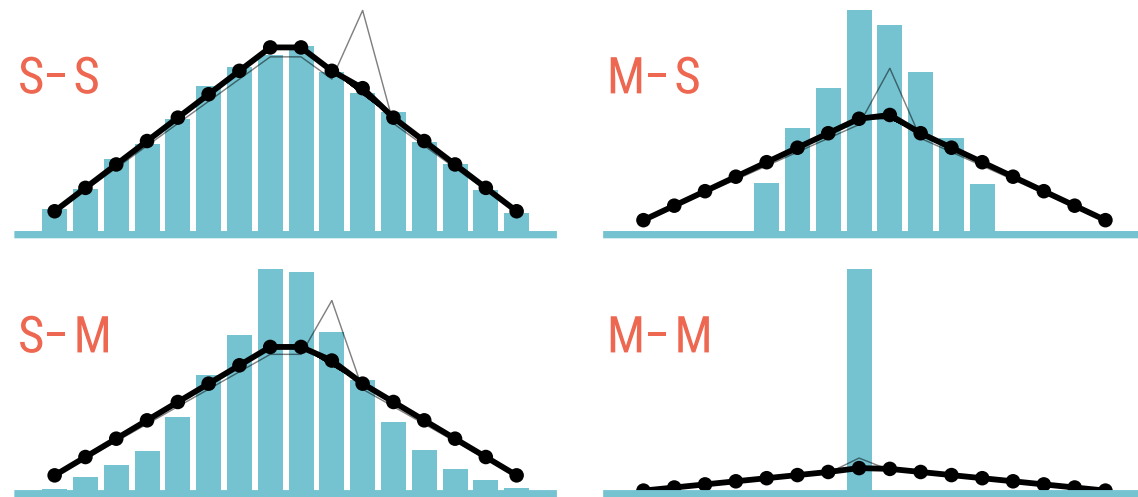


# Different strategies

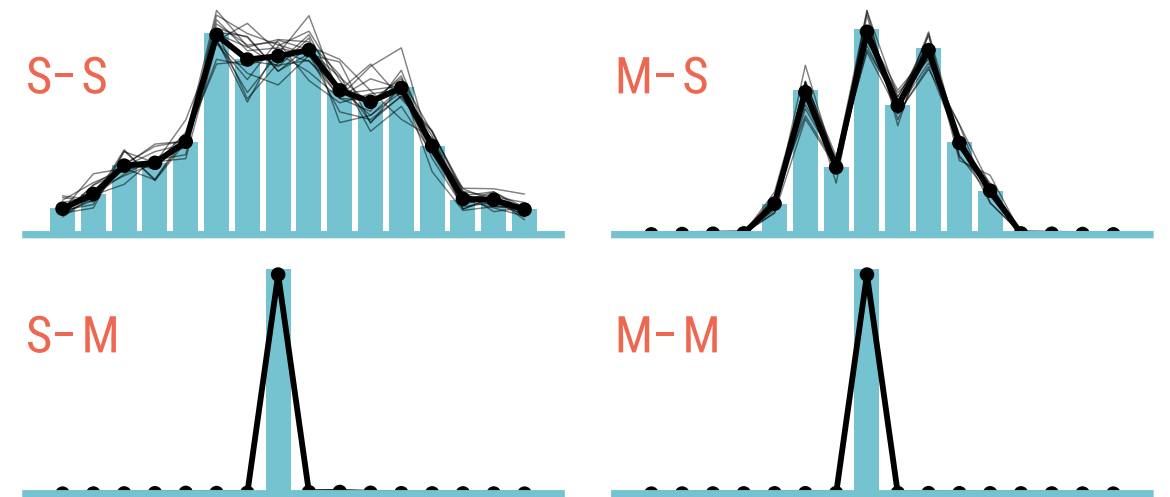


# Different strategies

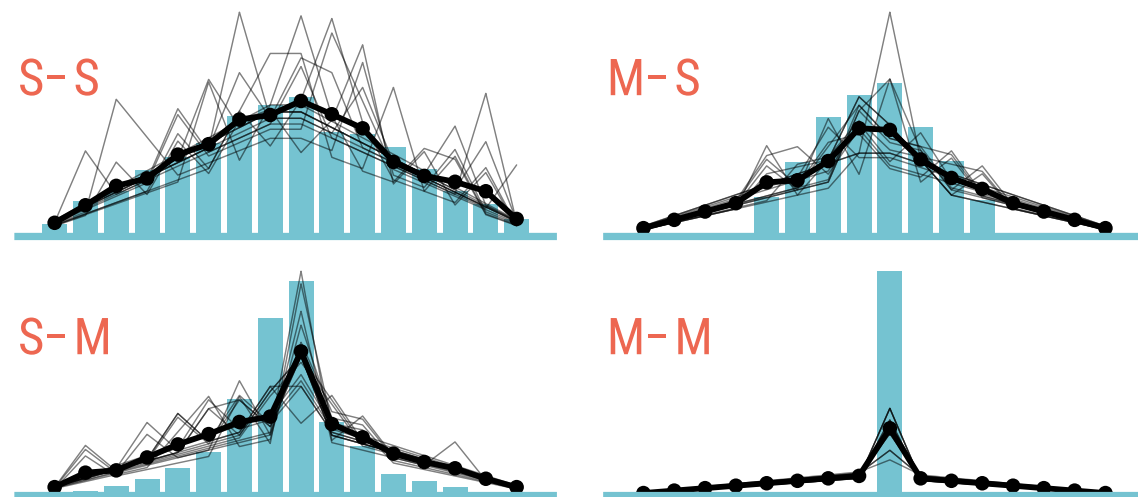
## A. Iterated learning ( $\gamma = 1$ )



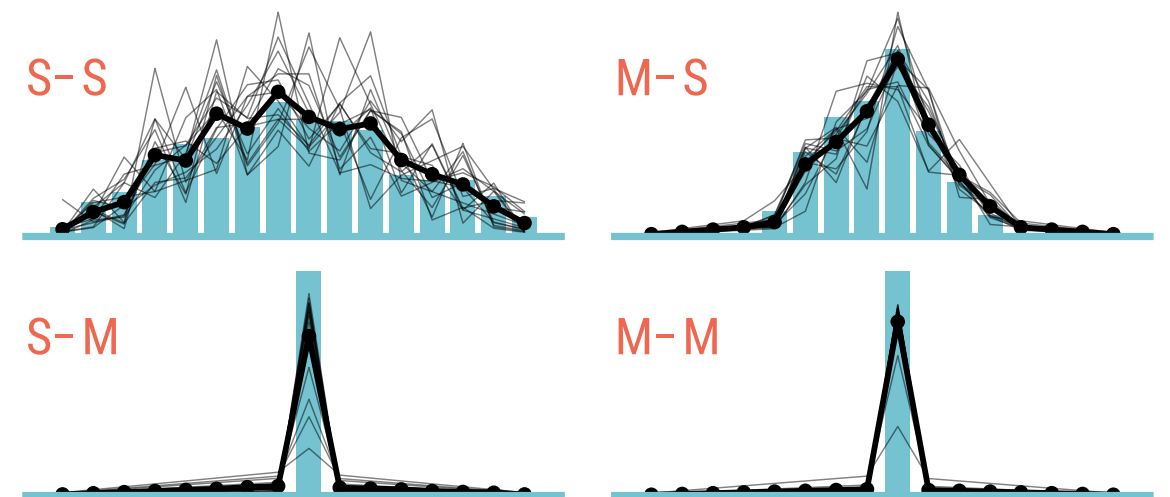
## B. Naming Game ( $\gamma = \infty$ )



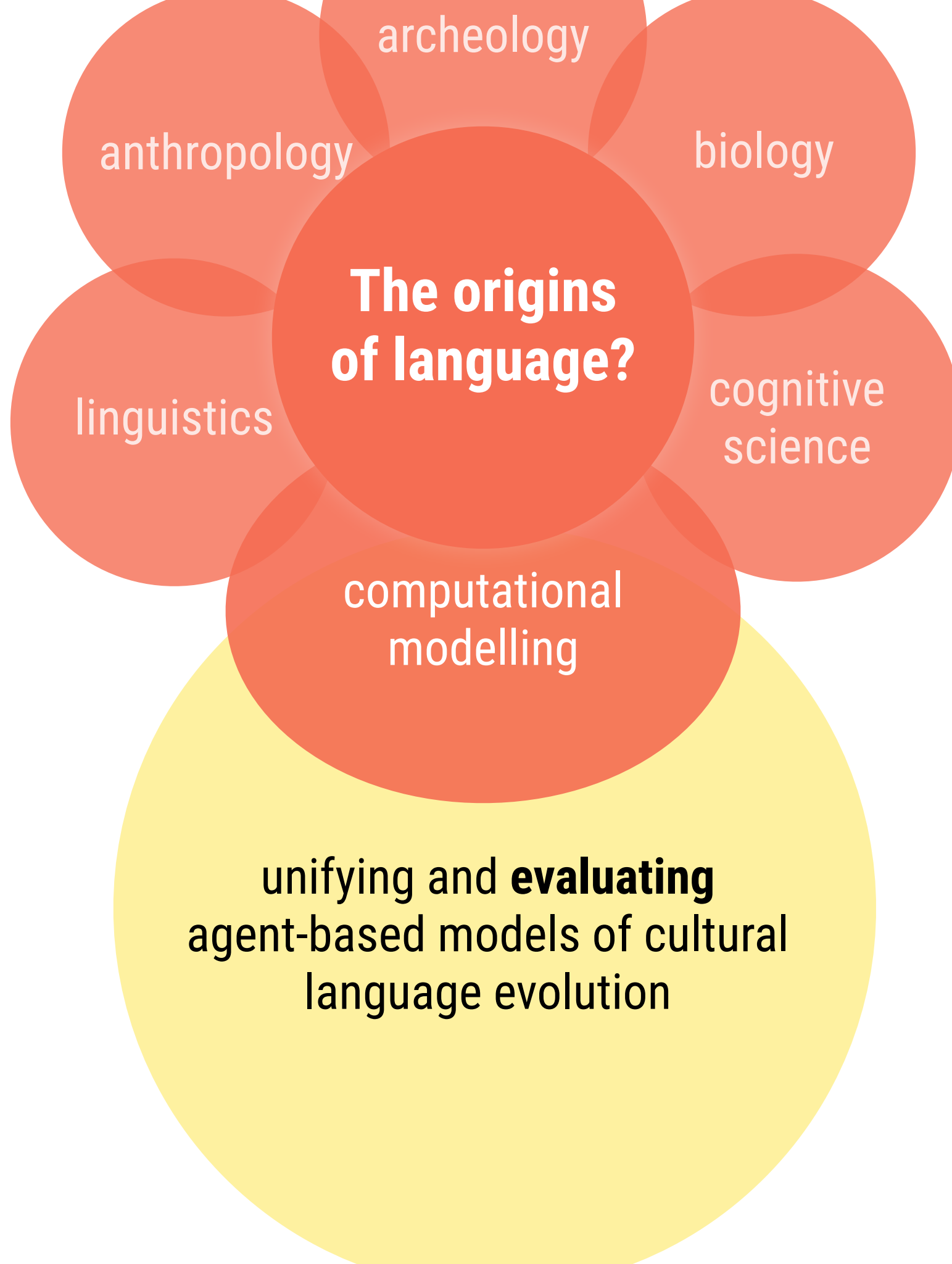
## C. Quick turnover ( $\gamma = 10$ )



## D. Medium turnover ( $\gamma = 100$ )



—●— Aggregate language  $\bar{\pi}$       — Expected language  $\pi$       ■ External language  $\psi$



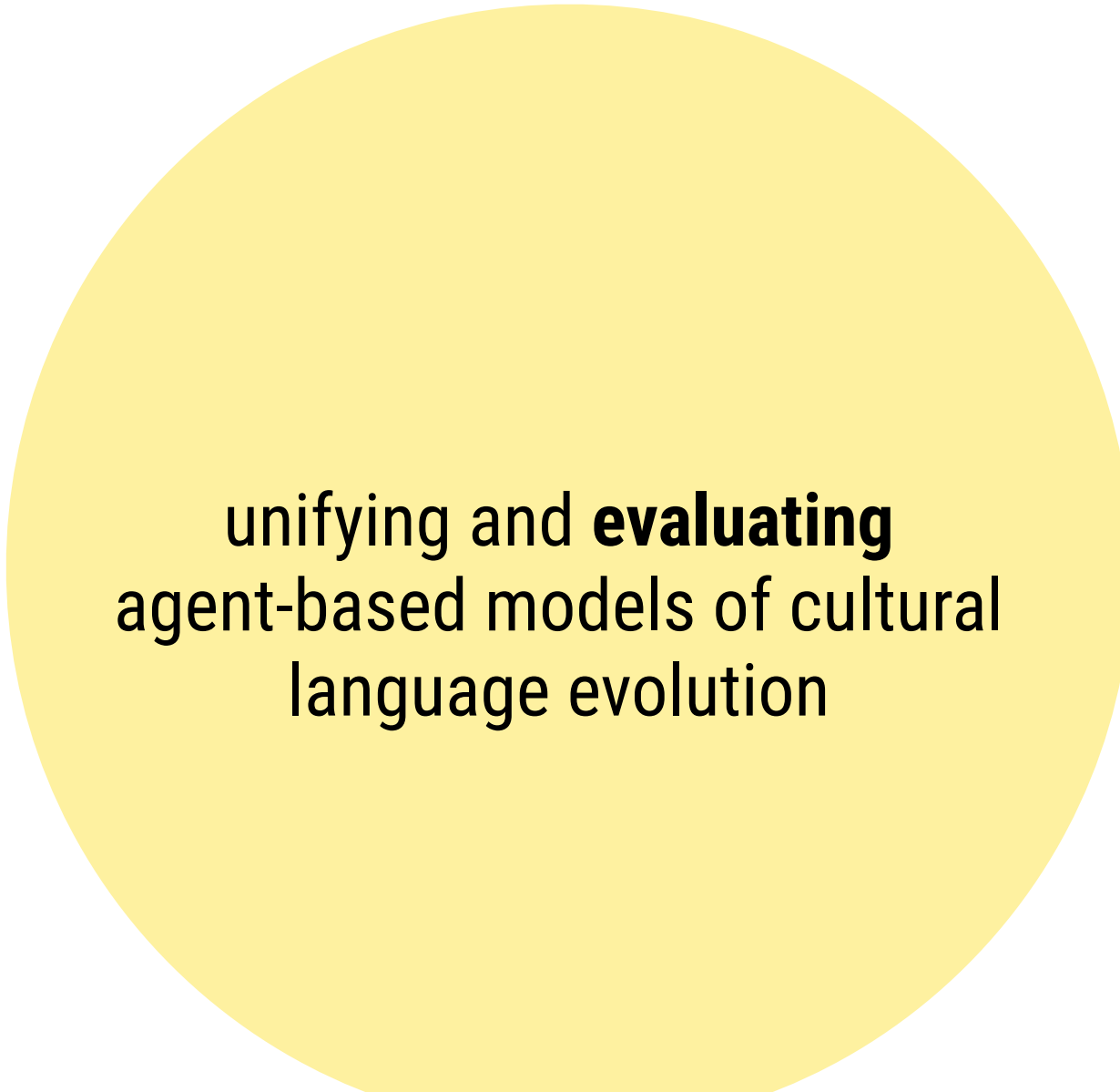
## Take home messages

Iterated learning and the naming game closely related:

language evolution through frequency tracking and innate biases.

Realistic?

Lineage-specific languages reflecting innate biases in the Bayesian naming game.



unifying and **evaluating**  
agent-based models of cultural  
language evolution





**The (Little) Tower of Babel** by **Pieter Bruegel the Elder** (c. 1563) oil on panel; 60 cm × 74.5 cm; Museum Boijmans Van Beuningen, Rotterdam